

# Calculus 1

## Real Numbers

$$N = \{ 1, 2, 3, 4, \dots \} \text{ Natural}$$

$$W = \{ 0, 1, 2, 3, 4, \dots \} \text{ Whole number}$$

$$Z = \{ \dots, -3, -2, -1, 0, 1, 2, 3, \dots \} \text{ integer}$$

$$Q = \left\{ \frac{a}{b}, a \in Z, b \in Z, b \neq 0 \right\}$$

Rational number

$$\frac{3}{0}$$

$$\frac{2}{1}$$

undefined

$$\sqrt{4} = 2$$

$$\sqrt{3} = 1.732 \dots$$

$$\sqrt{2} \text{ irrational}$$

$$\sqrt{5}$$

$\mathbb{R}$

real numbers

Rational

irrational

$\mathbb{R}$

$$= (-\infty, \infty)$$



interval

الفترات

$$(-\infty, \infty) = \mathbb{R}$$

1] closed interval

$$X = [3, 7]$$

$$\begin{aligned} 3 &\in X \\ 7 &\in X \end{aligned}$$

2] open interval

$$X = (3, 7)$$

$$3 \notin X \quad 3.06000001 \in X$$

$$7 \notin X$$

3] Sim-open

$$[3, 7)$$

$$(3, 7]$$

Properties of Real number

$$1] X + Y = Y + X$$

$$2] X + 0 = X$$

$$3] (X + Y) + Z = X + (Y + Z)$$

$$4] X - Y \neq Y - X$$

$$5] XY = YX$$

$$6] X \cdot 1 = X$$

$$7] X \cdot (Y \cdot Z) = (X \cdot Y) \cdot Z$$

$$X(Y + Z) = XY + XZ$$

$$\frac{X}{Y} \neq \frac{Y}{X}$$



# Set Notation

1] Intersection التقاطع

$$\{1, 2, 3\} \cap \{2, 4, 5\} = \{2\}$$

$A \cap B = B \cap A$

2] Union الاتحاد +

$$\{1, 2, 3\} \cup \{2, 4, 5\} = \{1, 2, 3, 4, 5\}$$

$A \cup B = B \cup A$

3] Difference الفرق

$$\overset{A}{\{1, 2, 3\}} - \overset{B}{\{2, 4, 5\}} = \{1, 3\}$$

$$A - B \neq B - A$$

$$A - B = \{1, 3\}$$

$$B - A = \{4, 5\}$$

4] supset

$$A = \{1, 2, 3\}$$

$$\{1\} \subseteq A$$

$$\{2, 3\} \subseteq A$$

$$\emptyset = \{ \} \text{ empty set}$$

$$A = \{1, 2, 3\}$$

$$2^n = 2^3 = 8$$

$$\emptyset, \{1\}, \{2\}, \{3\}, \{1, 2\}, \{1, 3\}$$

$$\{2, 3\}, \{1, 2, 3\}$$

Equation      المعادلات

$$x + 3 = 4$$
$$\boxed{x = 1}$$

$$2x + 4 = 7$$

$$2x = 7 - 4$$

$$2x = 3$$

$$\boxed{x = \frac{3}{2}}$$

$$4 \leq x + 3 \leq 7$$

$$4 - 3 \leq x + 3 - 3 \leq 7 - 3$$

$$1 \leq x \leq 4$$

$$\boxed{[1, 4]}$$

inequality      المتباينة

$$x + 3 < 4$$

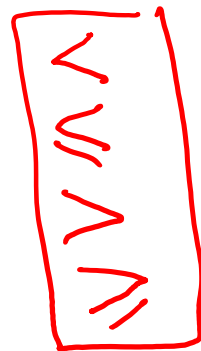
$$x < 4 - 3$$

$$\boxed{x < 1}$$

$$x \leq 1$$

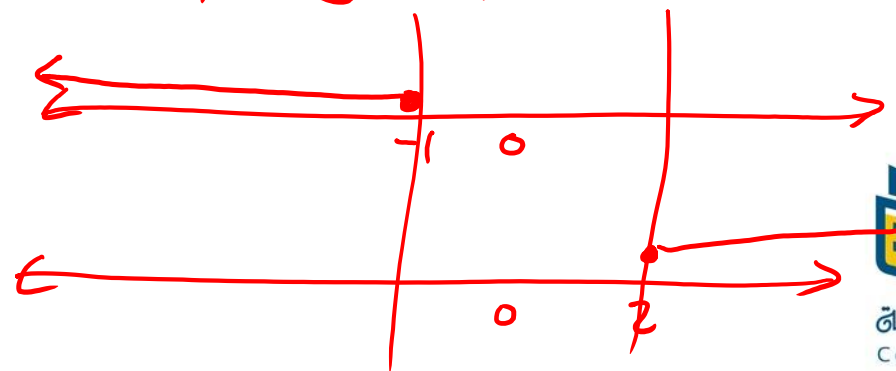
$$(-\infty, 1)$$

$$(-\infty, 1]$$



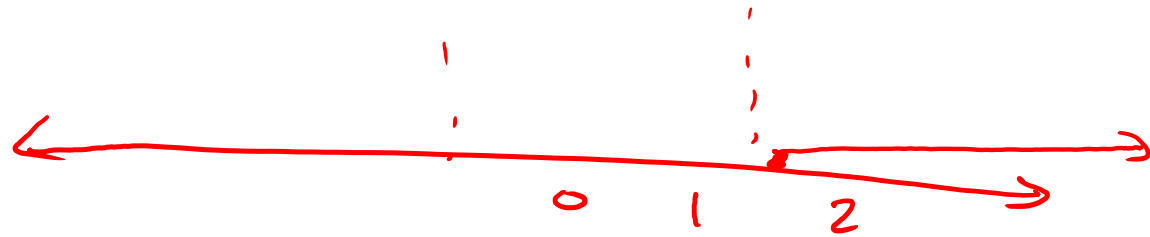
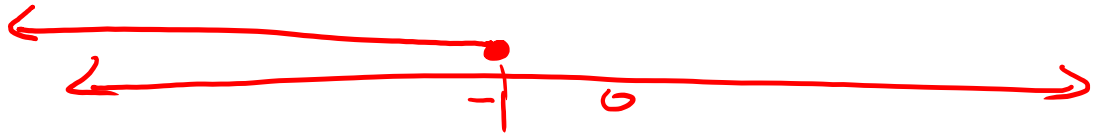
$$x \leq -1 \text{ and } x \geq 2$$

$$(-\infty, -1] \cap [2, \infty) = \emptyset$$



$$x \leq -1 \quad \text{or} \quad x \geq \frac{3}{2}$$

$$(-\infty, -1] \cup \left[\frac{3}{2}, \infty\right) = (-\infty, \infty) - (-1, \frac{3}{2})$$



$$(-\infty, 3] \cup [2, \infty) = (-\infty, \infty)$$

